

# High Power HF Filter Design

## With Applications to SO2R

Jeff Crawford, K0ZR

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# Preface

Without filters, radio communications would not be possible. Filters are responsible for segregating wanted frequency spans from those areas of the spectrum that are of no interest. The subject area of filters has a lengthy history commensurate with the earliest beginnings of radio.

Only those areas of filter theory important to HF filter design in the 1 MHz to 30 MHz frequency range are considered here. Many of the principles and techniques discussed have applicability to much higher frequencies, even microwave, however the manner in which the theories and principles are applied change significantly between 1 MHz and 1 GHz. The principles and methods advanced herein deal only with lumped element designs compared to *distributed* or *waveguide* forms which find application at frequencies considerably higher than HF.

The subject of filters may seem elementary upon first glance; after all a filter is just a succession of inductors and capacitors. Such an assessment would be highly incorrect in that the mathematics involved behind the scenes is formidable. This text strives to stay away from such deep theories and high level mathematics, even though some readers may form a different opinion upon their first review of this book. Consideration of some of the references such as Matthaei [6], Daryanani [4], Helszajn [64], and Knight [13] offer convincing evidence in support of the aforementioned statement regarding complexity.

This is not an ordinary book on filters in that most of the synthesis details are left to the many references available on the subject, some of which are found in the bibliography. Here, the concentration is on how to design and construct KW filters without having to go to the expensive NOS<sup>1</sup> doorknob capacitors that the majority of KW filter manufacturers use. NOS sources for doorknob capacitors have decreased in recent years and in the wake of the problems in Ukraine, the scarcity of such capacitors has grown more problematic. Through use of the multiple techniques described herein, the need for doorknob capacitors and/or high VAR<sup>2</sup> capacitors is considerably reduced allowing the designer to use less costly and far more plentiful multi-layer ceramic chip capacitors (MLCC).

The book begins with the introduction to Single Operator Two Radio (SO2R) in Chapter 1 and lays the framework for the essential elements of an SO2R station. Chapter 2 sets the stage for filter theory in general, however it does so by introducing some rather complex topics which may be too advanced for some readers; no need for worry due to the use of the ELSIE filter design program. Chapter 2 is included for completeness, however, if the reader chooses to bypass it, this should not impede his understanding and application of the remaining chapters. Chapter 3 discusses several important physics characteristics essential to filter design. One of the most

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<sup>1</sup>New Old Stock

<sup>2</sup>VAR =  $V_{\text{RMS}} \times I_{\text{RMS}}$

important chapters in the book, Chapter 4, discusses the electrical and behavioral characteristics of the components used to construct filters. Most of these principles are important from the milliwatt level up to kilowatt level. Chapter 5 does a comparison of seven different filter designs incorporating elliptic, Chebyshev, Constant-k, and m-derived topologies. These comparisons will help the reader formulate the differences to be expected across different filter families. Chapter 6 is a brief tutorial on circuit simulation in general, while Chapter 7 addresses requirements for heat dissipation to guarantee survival at high power and prolong filter life.

Chapter 8 is the foundation for KW-level filter design embraced throughout this book. Through the use of the powerful transform methods described here, ‘unbuildable’ filters become ‘buildable’, or the time-consuming design of many different inductor values can be simplified through the use of equal size inductors, just two benefits of the information contained in this chapter. The application level equations of the transforms are presented in Chapter 8, with the derivation of several Norton transforms and JK inverter equations relegated to a deeper treatise in the *Appendix*.

Chapters 9 and 10 should be of considerable interest should the reader take on the challenge of building his own KW-level bandpass filters. Chapter 9 deals with a design for 40m while Chapter 10 is dedicated to a 15m design. The two designs incorporate somewhat different approaches and serve to illuminate some of the techniques used by filter designers.

Chapter 11 concludes the primary part of the book, covering other aspects of filter construction not presented elsewhere. The principal topics covered include troubleshooting and filter augmentation with tuned coaxial stubs. A failure of several silver mica capacitors in the KØZR 80m filter are described and the troubleshooting process used in its repair outlined.

This book is the outcome of the author’s filter design efforts which began in 2017. Upon venturing into SO2R in 2016, he initially used a variety of coaxial stubs [1] to improve attenuation of neighboring bands by ~ 20 - 25 dB. Due to 10m, 15m, and 20m elements all residing on the same boom of his C31XR tribander, more isolation was desired. The C31XR can be used in a single-feed configuration, although three separate feedlines and driven element modifications are in use for today’s SO2R installation. The amount of coupling between 15m and 20m, which is very high, is a byproduct of the original coupled-sleeve approach used in the single-feed system of the C31XR. This Yagi design characteristic begs for more isolation between 20m and 15m in the SO2R station.

The reader will judge for himself whether the full disclosure approach taken in the book is helpful. The techniques and processes which are known to work are discussed at length, however things that do not work or resulted in failure are described as well. The author believes learning takes place in both successful and challenging situations. Chapters 9 and 10 share both types of experiences during the design and construction of two different filters.

The author’s venture into amateur radio began at age 13 when he obtained a Drake 2C receiver with the intention of becoming a more serious SWL (shortwave listener). The receiver covered the HF amateur bands; ham radio was discovered in short order. One afternoon a very strong signal on 75m became the center of attention; it was WAØRDZ who, with the help of the author’s father, was identified as Ed Askew, a local farmer. Shortly thereafter, Ed became the author’s ham radio mentor, which led to his becoming licensed as WAØZRT at age 15.

While in college, a vision of going to medical school transitioned to returning to the family business in Sidney, Iowa, where the author practiced as a funeral director for three years. It was

at the end of this period that electrical engineering came knocking, leading to a BSEE from the University of Nebraska-Lincoln, followed by an MSEE from the University of Southern California. The author's career has been RF/microwave design for satellites in support of the intelligence community for the past 40 years. Retirement is yet to be considered although the tug is getting stronger.

It is fitting to give credit where credit is due; this begins with the author's wife Cheryl. In December 2021, the author announced his desire to write this book. While his XYL knew this would be a large commitment of time and energy, she knew it was an important goal and her support has been unwavering over the many months of this project. She spent many hours reviewing the manuscript and her efforts have improved this book overall. Also W4RN, a great friend, the type of friend a person is lucky to find once in a lifetime, has been an omnipresent encourager for many years. His influence in the application of tuned stubs, dedicated Caribbean-facing Yagis for 10, 15, and 20m, contesting hints, and introduction to RTTY contesting have been invaluable.

Amateur radio and his electrical engineering career have strengthened the author's faith in God and the Bible. Both avocations have given him more insight into the complex world around us and reinforced his belief that its existence is possible only through a supreme Creator.

It is the author's hope that should the reader embark on constructing his own filters, this book will help him gauge the complexity involved, prepare him for what lies ahead, and help ensure his success in his DIY project. The satisfaction of completing such an undertaking is worth the effort required to cross the finish line.

Jeff Crawford, K0ZR